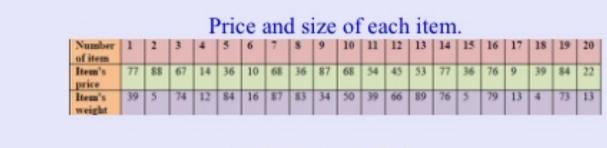
# What else?

# **Knapsack Problem**



Fitness vs. Generation.



The best combination with maximum total price.

Item	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
Number of items	4	5	0	2	0	1	0	0	4	5	4	0	0	1	4	0	0	4	1	4
Item's price	308	440	0	28	0	10	0	0	348	340	216	0	0	77	144	0	0	156	84	88

Yulia Lishko (2014)

## **Dimension Reduction**

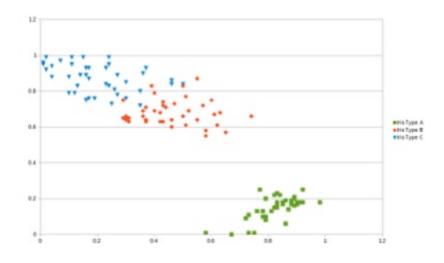
#### (1) A classification of iris flowers



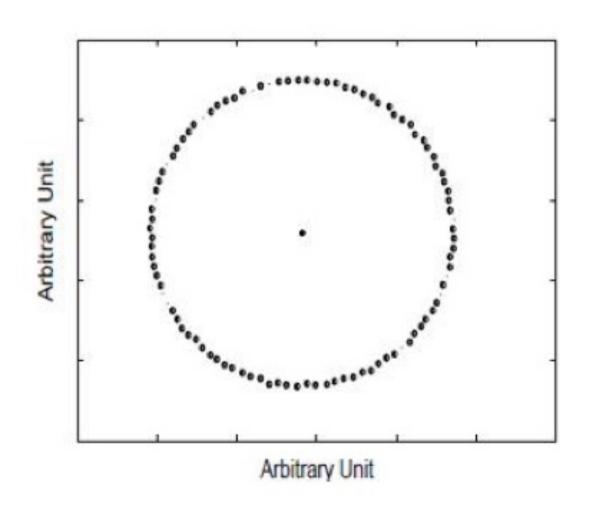




$x_1$	$x_2$	$x_3$	$x_4$	class
5.1	3.5	1.4	0.2	1 (Setosa)
4.9	3.0	1.4	0.2	1 (Setosa)
4.7	3.2	1.3	0.2	1 (Setosa)
7.0	3.2	4.1	1.4	2 (Versicolor)
6.4	3.2	4.5	1.5	2 (Versicolor)
6.9	3.1	4.9	1.5	2 (Versicolor)
5.8	2.7	5.1	1.9	3 (Virginica)
7.1	3.0	5.9	2.1	3 (Virginica)
6.3	2.9	5.6	1.8	3 (Virginica)



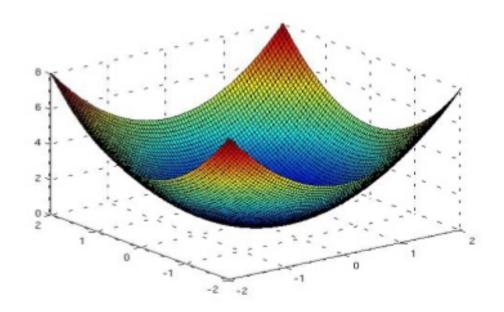
(2) 100 points from surface of hyper sphere in 49<sup>2</sup> = 2401 dimensional space



# **3-D Function Optimization**

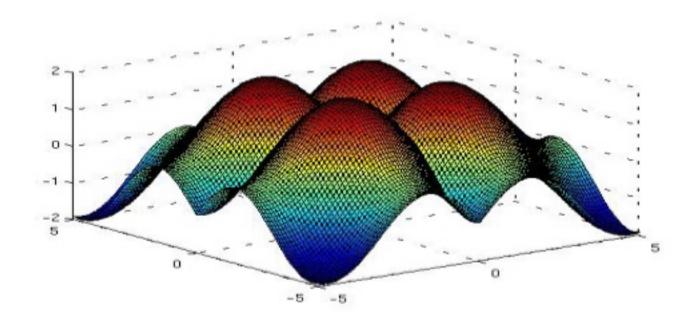
#### (1) Sphere model

$$z = x^2 + y^2$$

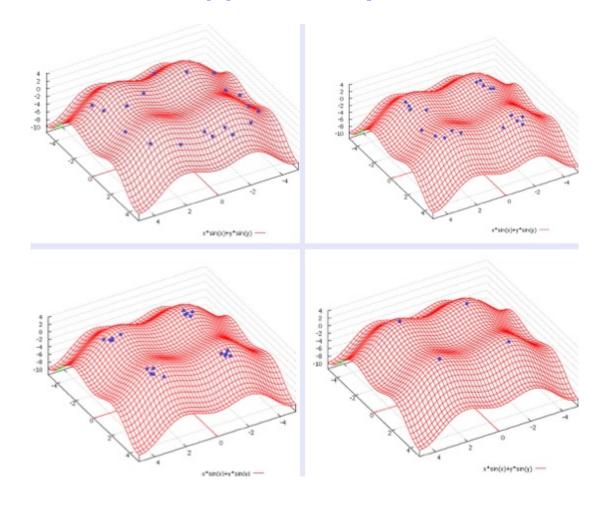


# (2) 3-D Schwefel function

$$z = x \sin(|x|) + y \sin(|y|)$$



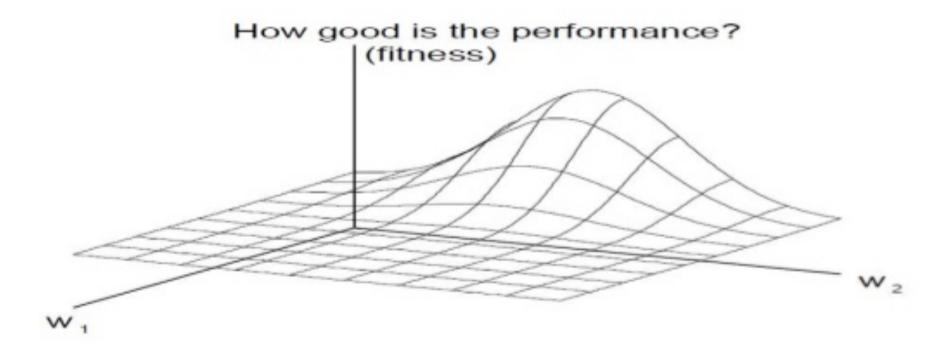
# (3) An example



### Random Mutation Hill-climbing

- (1) choose a string at random and call this current-hilltop
- (2) choose a locus at random to flip. If the flip leads to an equal or higher fitness then set current-hilltop to the resulting string
- (3) goto step (2) until an optimum string has been found or until a maximum number of evaluations have been performed.
- (4) return the current-hilltop

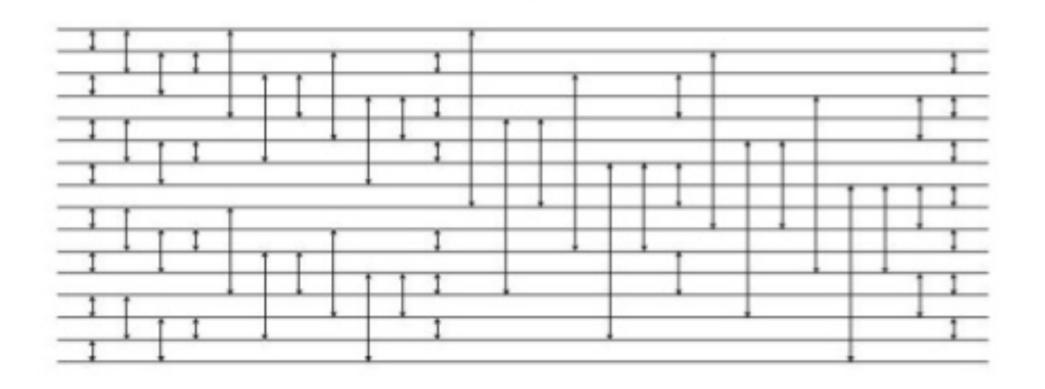
# A conceptual plot of fitness value defined on a fictitious 2-D space



# A needle in a hay stack problem



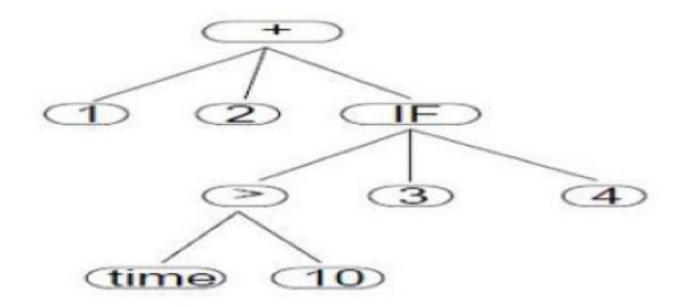
Ex. Sorting algorithm by Knuth et. al (1964)
63 Comparisons



#### **Evolution of Tree Structure**

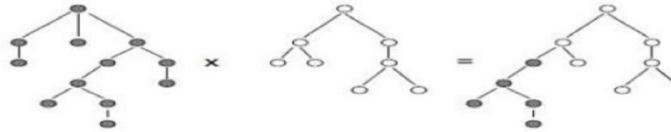
Prgramming in LISP which can be represented by tree such as

(+ 1 2 (IF (> time 10) 3 4))

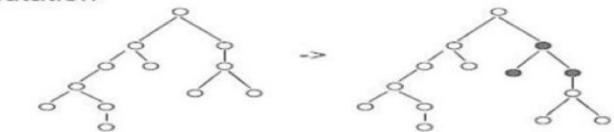


#### Its crossover & mutation





#### mutation



#### **Evolution under two Fitness Functions**

