## What else?

## Knapsack Problem

Price and size of each item.

| Number <br> of item | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Item's <br> praice | 77 | 88 | 67 | 14 | 36 | 10 | 68 | 36 | 87 | 68 | 34 | 45 | 53 | 77 | 36 | 76 | 9 | 39 | 84 | 22 |
| Item's <br> weight | 39 | 5 | 74 | 12 | 84 | 16 | 87 | 83 | 34 | 50 | 39 | 66 | 89 | 76 | 5 | 79 | 13 | 4 | 73 | 13 |

Fitness vs. Generation.


The best combination with maximum total price.

| Itum | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number <br> of items | 4 | 5 | 0 | 2 | 0 | 1 | 0 | 0 | 4 | 5 | 4 | 0 | 0 | 1 | 4 | 0 | 0 | 4 | 1 | 4 |
| Item's <br> price | 308 | 440 | 0 | 28 | 0 | 10 | 0 | 0 | 348 | 340 | 216 | 0 | 0 | 77 | 144 | 0 | 0 | 156 | 84 | 88 |

Yulia Lishko (2014)

## Dimension Reduction

(1) A classification of iris flowers


| $x_{1}$ | $x_{2}$ | $x_{3}$ | $x_{4}$ | class |
| :---: | :---: | :---: | :---: | :---: |
| 5.1 | 3.5 | 1.4 | 0.2 | 1 (Setosa) |
| 4.9 | 3.0 | 1.4 | 0.2 | 1 (Setosa) |
| 4.7 | 3.2 | 1.3 | 0.2 | 1 (Setosa) |
| $\cdots$ | $\cdots$ | $\ldots$ | $\cdots$ | $\ldots$ |
| 7.0 | 3.2 | 4.1 | 1.4 | 2 (Versicolor) |
| 6.4 | 3.2 | 4.5 | 1.5 | 2 (Versicolor) |
| 6.9 | 3.1 | 4.9 | 1.5 | 2 (Versicolor) |
| $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ |
| 5.8 | 2.7 | 5.1 | 1.9 | 3 (Virginica) |
| 7.1 | 3.0 | 5.9 | 2.1 | 3 (Virginica) |
| 6.3 | 2.9 | 5.6 | 1.8 | 3 (Virginica) |
| $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ |


(2) 100 points
from surface of hyper sphere in 49^2 $=2401$ dimensional space


## 3-D Function Optimization

(1) Sphere model

$$
z=x^{2}+y^{2}
$$


(2) 3-D Schwefel function

$$
z=x \sin (|x|)+y \sin (|y|)
$$


(3) An example


## Random Mutation Hill-climbing

(1) choose a string at random and call this current-hilltop
(2) choose a locus at random to flip. If the flip leads to an equal or higher fitness then set current-hilltop to the resulting string
(3) goto step (2) until an optimum string has been found or until a maximum number of evaluations have been performed.
(4) return the current-hilltop

A conceptual plot of fitness value defined on a fictitious 2-D space


## A needle in a hay stack problem

Ex. Sorting algorithm by Knuth et. al (1964)

## 63 Comparisons



## Evolution of Tree Structure

Prgramming in LISP which can be represented by tree such as
$(\rightarrow 12(1 F(>$ time 10$) 34))$


Its crossover \& mutation
crossover

mutation


## Evolution under two Fitness Functions





