

**CCOD**  
**Lab 7 13.10.2016**  
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Below you can see 3 Gaussian Membership Function of small, medium and large x-y coordinate:



I've created 3 rules for each family A, B, C:

Rule 1: If  $x_1=\text{large}$ ;  $x_2=\text{large}$ ;  $x_3=\text{small}$ ;  $x_4=\text{small}$ , then Family A.

Rule 2: If  $x_1=\text{large}$ ;  $x_2=\text{large}$ ;  $x_3=\text{large}$ ;  $x_4=\text{medium}$ , then Family B.

Rule 3: If  $x_1=\text{large}$ ;  $x_2=\text{medium}$ ;  $x_3=\text{large}$ ;  $x_4=\text{large}$ , then Family C.

Data to evaluate

**Iris Flower Database to validate**

Setosa				Versicolor				Virginica			
$x_1$	$x_2$	$x_3$	$x_4$	$x_1$	$x_2$	$x_3$	$x_4$	$x_1$	$x_2$	$x_3$	$x_4$
0.65	0.80	0.20	0.08	0.89	0.73	0.68	0.56	0.80	0.75	0.87	1.00
0.62	0.68	0.20	0.08	0.81	0.73	0.65	0.60	0.73	0.61	0.74	0.76
0.59	0.73	0.19	0.08	0.87	0.70	0.71	0.60	0.90	0.68	0.86	0.84
0.58	0.70	0.22	0.08	0.70	0.52	0.58	0.52	0.80	0.66	0.81	0.72
0.63	0.82	0.20	0.08	0.82	0.64	0.67	0.60	0.82	0.68	0.84	0.88
0.68	0.89	0.25	0.16	0.72	0.64	0.65	0.52	0.96	0.68	0.96	0.84
0.58	0.77	0.20	0.12	0.80	0.75	0.68	0.64	0.62	0.57	0.65	0.68
0.63	0.77	0.22	0.08	0.62	0.55	0.48	0.40	0.92	0.66	0.91	0.72

Below you can find an example of calculation for next data:

Setosa				
$x_1$	$x_2$	$x_3$	$x_4$	$x_1$
0.65	0.80	0.20	0.08	0.89

To detect flower we need to find Y value and use next comparisons

$$y = \begin{cases} 1 & \text{A if } \hat{y} < 1.5 \\ 2 & \text{B if } 1.5 \leq \hat{y} < 3.0 \\ 3 & \text{C if } 3.0 \leq \hat{y} \end{cases}$$

Below you can see formula for Y

$$y_j = \frac{\sum_{k=1}^H (M_k(\mathbf{x}) \cdot g_k)}{\sum_{k=1}^H M_k(\mathbf{x})}$$

where

$$M_k(\mathbf{x}) = \prod_{i=1}^N \mu_{ik}(x_i)$$

where  $\mu_{ik}$  is  $i$ -th attribute of  $k$ -th rule

For calculating  $\mu$  we will use next formula:

$$\mu(x) = \exp\left\{-\frac{(x - avg)^2}{\sigma^2}\right\}$$

For small we will use:

```
function small(x) {
  return Math.exp(-((x - 0.1556) * (x - 0.1556)) / 0.00447);
};
```

For medium:

```
function medium(x) {
  return Math.exp(-((x - 0.6019) * (x - 0.6019)) / 0.004);
};
```

For large:

```
function large(x) {
    return Math.exp(-((x - 0.806) * (x - 0.806)) / 0.006);
};
```

We have all the data. So, let's find M1, M2 and M3:

Rule 1: If  $x_1=large$ ;  $x_2=large$ ;  $x_3=small$ ;  $x_4=small$ , then Family A.

$$\mu_1 = 0.017318153368134238$$

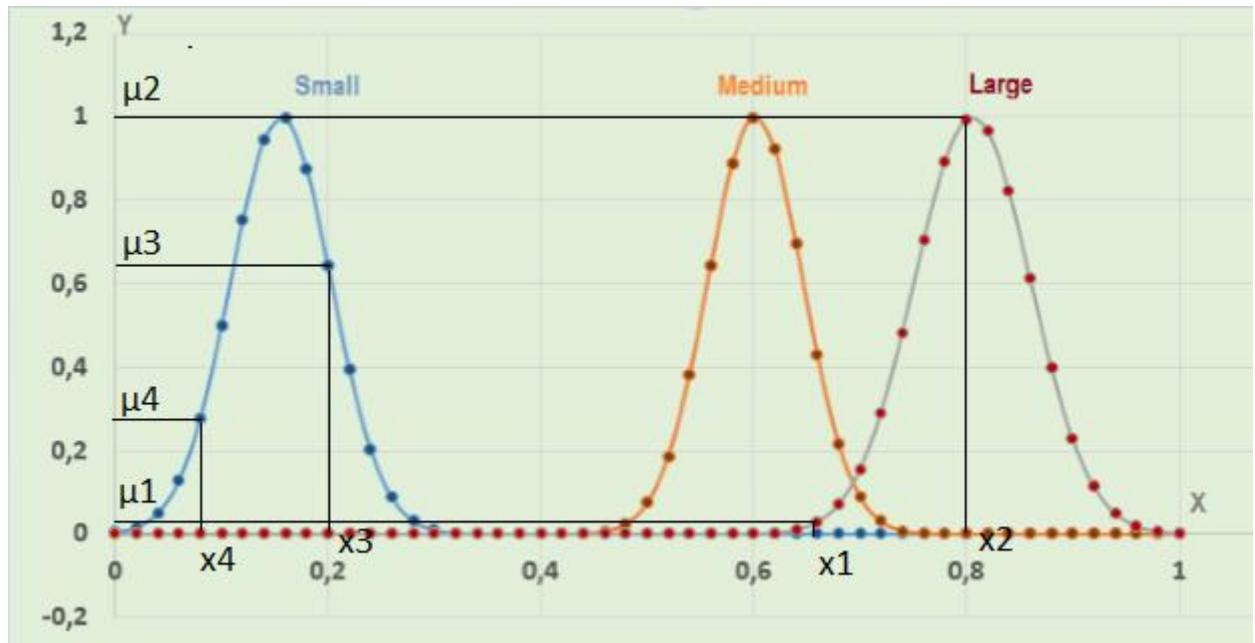
$$\mu_2 = 0.9940179640539353$$

$$\mu_3 = 0.643379752487798$$

$$\mu_4 = 0.27842570409799405$$

$$M_1 = \mu_1 * \mu_2 * \mu_3 * \mu_4 = 0.0030836753435$$

You can also find  $\mu$  from the graph, but it's not a good idea. The  $\mu$ 's value can be very small.



Rule 2: If  $x_1=large$ ;  $x_2=large$ ;  $x_3=large$ ;  $x_4=medium$ , then Family B.

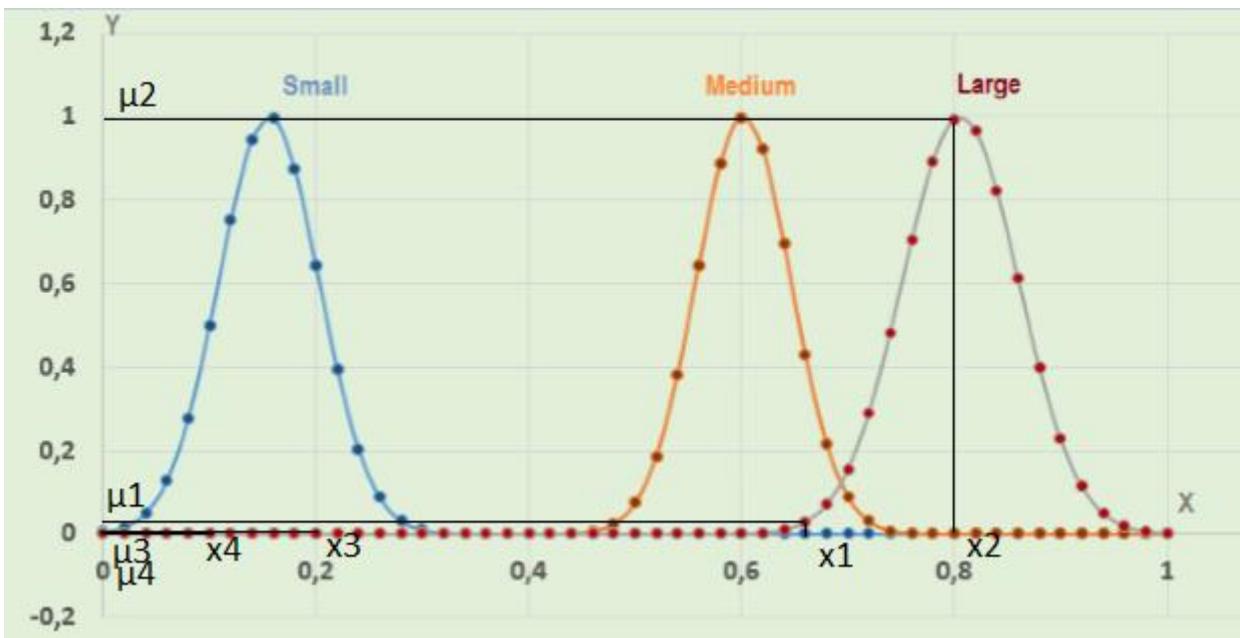
$$\mu_1 = 0.017318153368134238$$

$$\mu_2 = 0.9940179640539353$$

$$\mu_3 = 2.6216332747033475e-27$$

$$\mu_4 = 2.671527189077588e-30$$

$$M_2 = \mu_1 * \mu_2 * \mu_3 * \mu_4 = 1.205666943189679e-58$$



Rule 3: If  $x_1=\text{large}$ ;  $x_2=\text{medium}$ ;  $x_3=\text{large}$ ;  $x_4=\text{large}$ , then Family C.

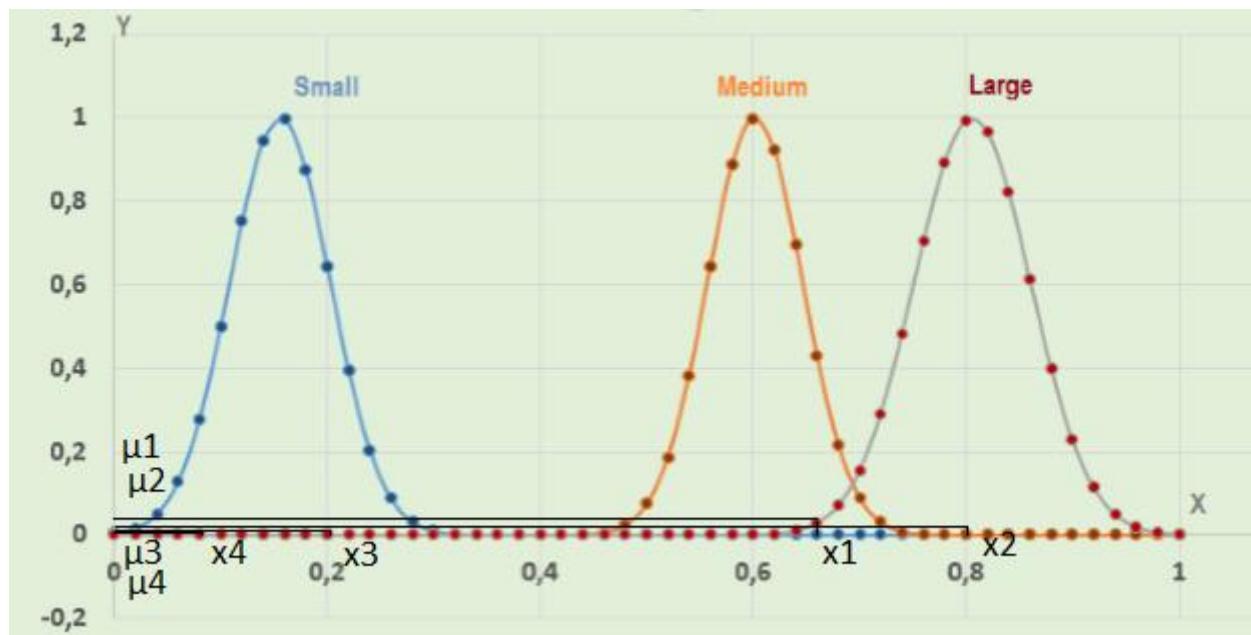
$$\mu_1 = 0.017318153368134238$$

$$\mu_2 = 0.000054850322038625596$$

$$\mu_3 = 2.6216332747033475e-27$$

$$\mu_4 = 7.062637934056824e-39$$

$$M_3 = \mu_1 * \mu_2 * \mu_3 * \mu_4 = 1.7588129171190555e-71$$



Using next formula, we can calculate  $Y$ :

$$y_j = \frac{\sum_{k=1}^H (M_k(\mathbf{x}) \cdot g_k)}{\sum_{k=1}^H M_k(\mathbf{x})}$$

.

$$Y = 1.0$$

$Y < 1.5$ , so **A** flower is detected.

Below you can see evaluated rules

Data №:	Family A	Family B	Family C	Result:
Nº 1	A	B	C	Good
Nº 2	A	B	C	Good
Nº 3	A	B	C	Good
Nº 4	A	C	C	Not Good
Nº 5	A	B	C	Good
Nº 6	A	B	C	Good
Nº 7	A	B	C	Good
Nº 8	A	B	C	Good
Success Rate:	100%	87.5%	100%	87.5%