

A-mesa-in-desert vs a-needle-in-haystack:

**A fitness landscape on weight space
of an application using spiking neurons
under rate coding.**

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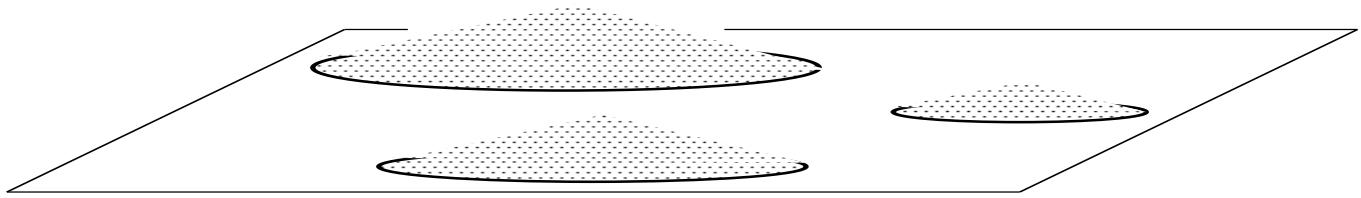
We came accross
an extremely difficult
PEAK
to be searched for

in a
FITNESS LANDSCAPE

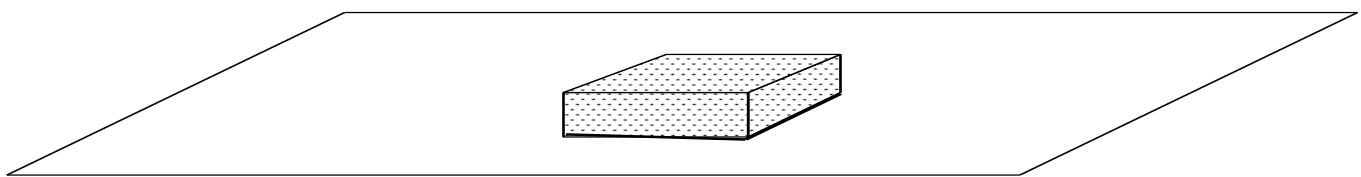
explored by an
EVOLUTIONARY COMPUTATION

□ A reason for the title — A mesa in desert

(a)



(b)



To realize an
ASSOCIATIVE MEMORY
we use
SPIKING NEURONS
whose learning is by
EVOLUTIONARY COMPUTATIONS.

□ Contents

1. What is Associative Memory?

- Traditional Model by Hopfield.

vs.

- A Model using Spiking Neurons.

2. Can we evolve Spiking Neurons?

- We study it by observing Fitness Landscape.

(cont'd)

3. Results of our Experiments.

- Let's see a downhill walk from Hebb's peak!
- Can we hillclimb again?
- Can Baldwin Effect help us to search?

4. Summary & Conclusions.

□ **Associative Memory:**

- **stores patterns**
 - in a distributed way (among neurons),
- **recalls patterns**
 - from noisy and/or partial input.

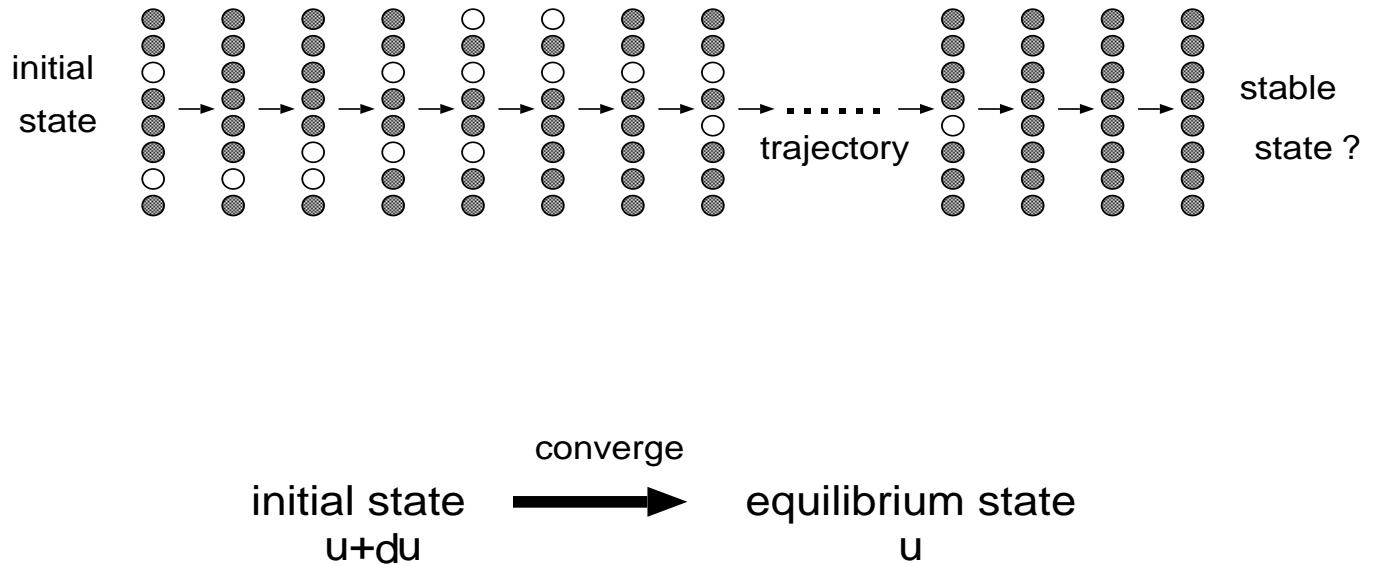
↓ i.e.

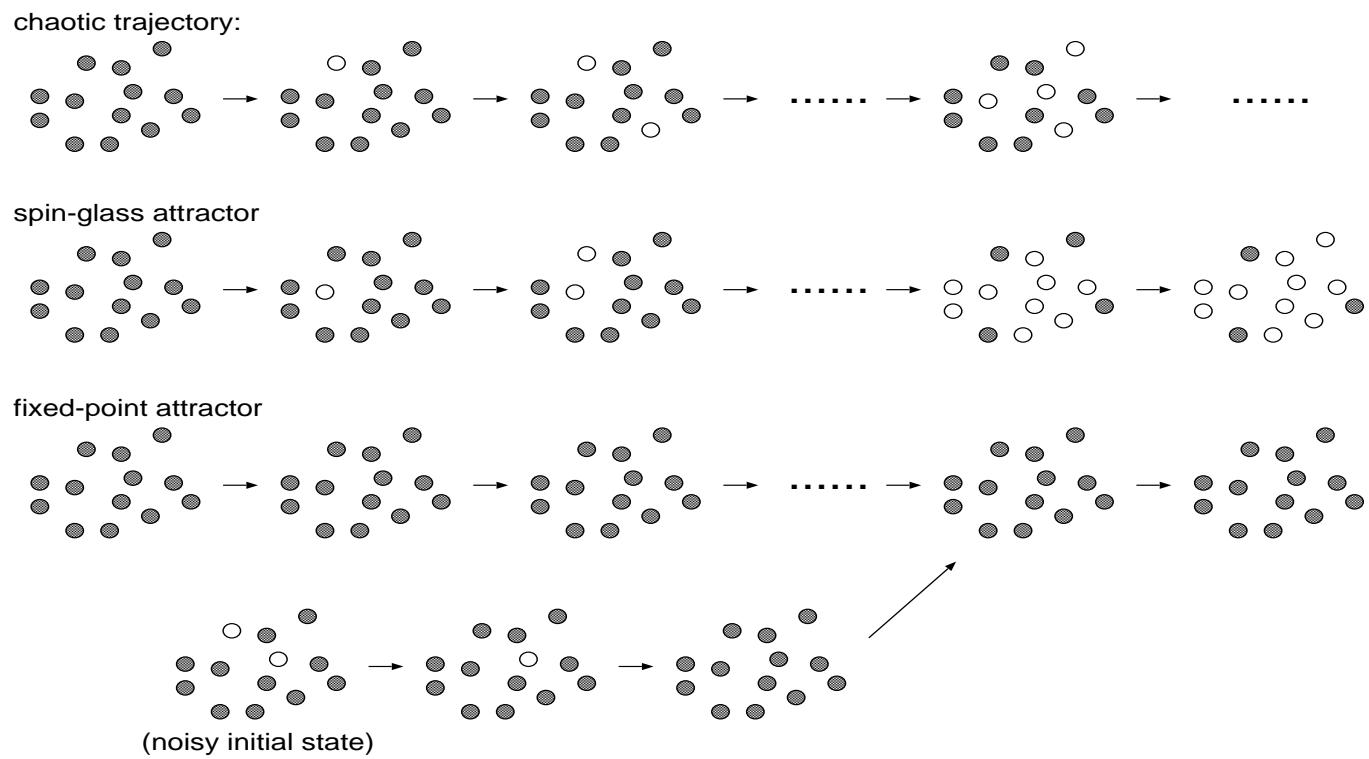
- **gives us**
 - perfect recollection from imperfect information

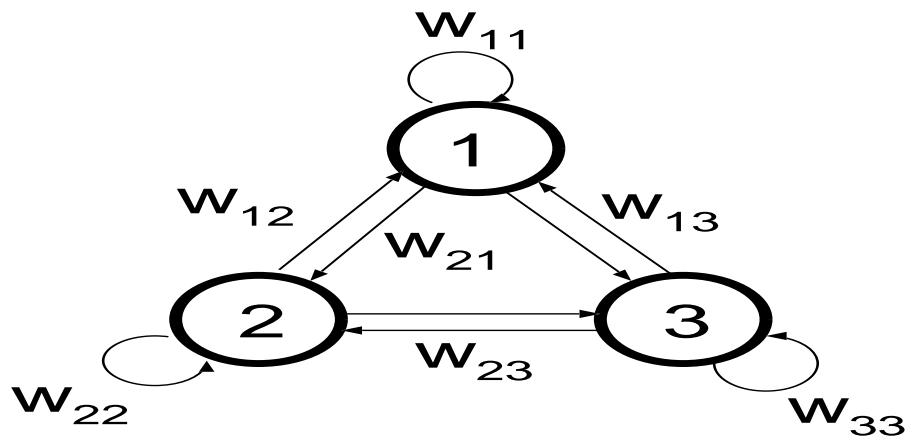
□ **The Associative Memory can be realized with:**

- Fully-connected Neural Network Model
(Hopfield type)
- Artificial Immune System Model
- Spiking Neurons
(To be more biologically plausible)
- etc.

associative memory = dynamical system





A Schematic Diagram of the Hopfield Model

□ State Transition of the Hopfield Model

$$s_i(t+1) = \operatorname{sgn}\left(\sum_j^N w_{ij} s_j(t)\right)$$

□ Hebbian Weights

$$w_{ij} = \frac{1}{N} \sum_{\mu=1}^p \xi_i^\mu \xi_j^\mu, \quad (i \neq j), \quad w_{ij} = 0.$$

(To store p patterns: $\mathbf{x}^\mu = (\xi_1^\mu, \xi_2^\mu, \dots, \xi_N^\mu)$ $\mu = 1, 2, \dots, p$)

□ **Hopfield Model has a Crucial Drawback.**

- N neurons store only $2N$ patterns at most (Gardner).

$$p < 2N.$$

□ **From the Hopfield Model to Spiking Neuron Model**

**Influence from other neurons
via
ELECTRIC CURRENTS**



**changes
MEMBRANE VOLTAGE
of the neuron.**

(cont'd)

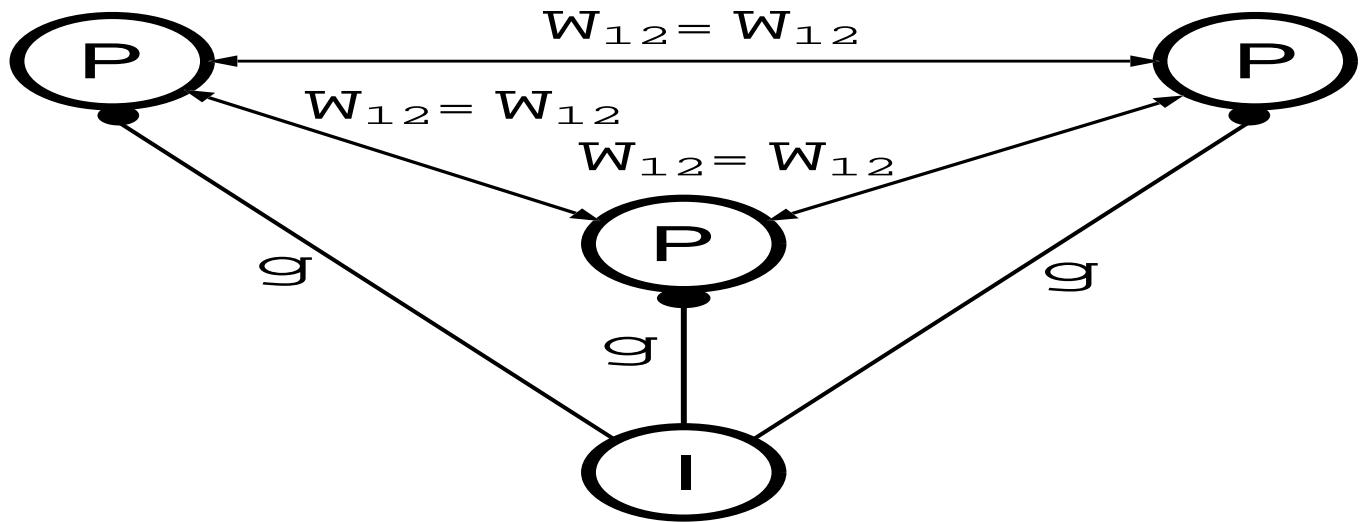


If it exceeds a threshold



**the neuron emits
a SPIKE.**

□ Pyramidal Cells & Interneurons



PYRAMIDAL CELL

||
(positive current)
↓↓

PYRAMIDAL CELL

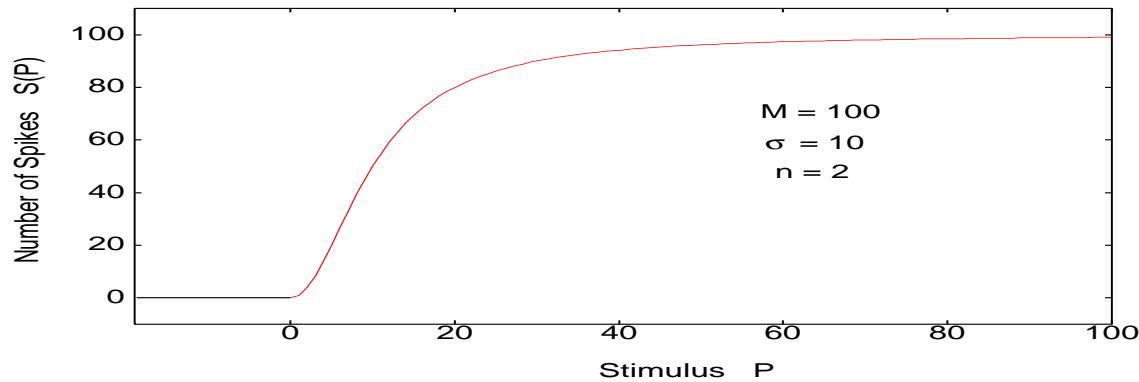
↑↑
(negative current)
||

INTERNEURON

□ Response of a Single Neuron to an External Stimulus:

- Spike rate vs stimuli (Naka-Rushton function)

$$S(P) = \begin{cases} MP^n / (\sigma^n + P^n) & \text{if } P \geq 0 \\ 0 & \text{if } P < 0 \end{cases}$$



(cont'd)

- **Spike rate under time-variant stimulus:**

$$\frac{dr(t)}{dt} = \frac{1}{\tau}(-r(t) + S(P))$$

□ Response of Multiple Neurons

• Stimulus to a Pyramidal Cell

$$P_i = (\sum_{j=1}^N w_{ij} \cdot R_j - g \cdot G)_+^2$$

of

$$S(P_i) = MP_i^n / (\sigma^n + P_i^n)$$

(cont'd)

- Spiking Ratio of a Pyramidal Cell

$$\frac{dr}{dt} = \frac{1}{\tau}(-r + MP^n/(\sigma^n + P^n))$$

becomes

$$\tau_R \frac{dR_i}{dt} = -R_i + \frac{100(\sum_{j=1}^N w_{ij} R_j - 0.1G)_+^2}{100 + (\sum_{j=1}^N w_{ij} R_j - 0.1G)_+^2}$$

(cont'd)

- **Spiking Ratio of Interneuron**

$$\tau_G \frac{dG}{dt} = -G - 0.07 \sum_{j=1}^N R_i$$

How to encode patterns?

$$\xi_i = \begin{cases} 1 & \text{if } R_i \geq M/2 \\ 0 & \text{if } R_i < M/2 \end{cases}$$

⇒ Rate Coding

GA Implementation:

1. Represent a series of w_{ij} as a *population* of strings (*chromosome*).

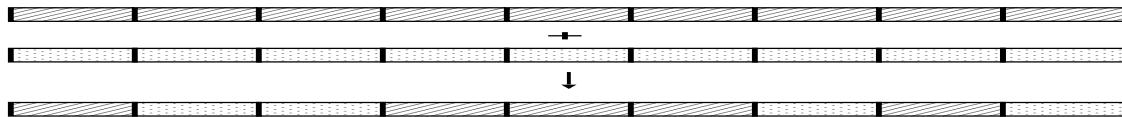
W11	W12	W13	...	W21	WN1	...	WNN
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2. Evaluate *fitness* by “How good is each individual?”
3. Generate an initial *population* at random.

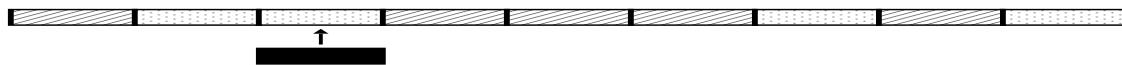
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4. Evolve them with

- *Selection*
- *Crossover*

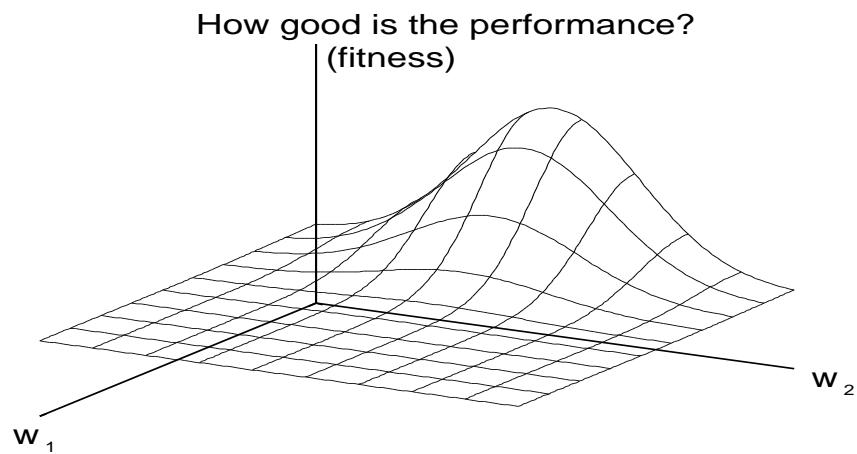


- *Mutation*



5. Better Solutions from *generation* to *generation*.

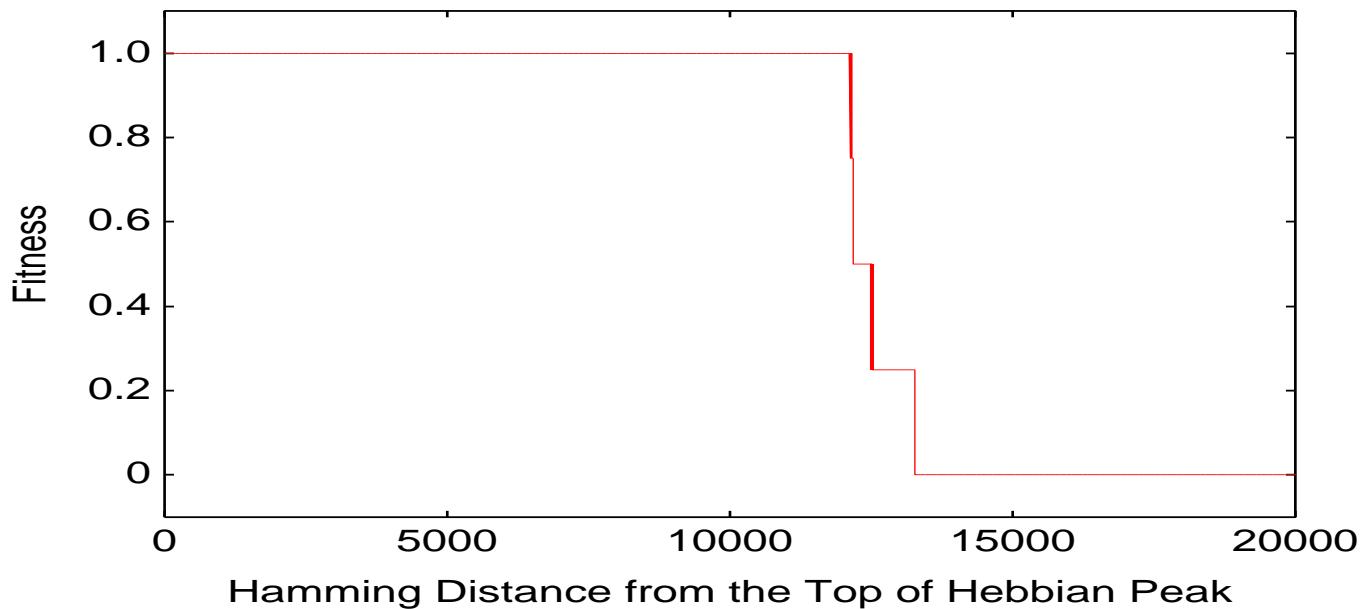
□ A Conceptual Illustration of Fitness Landscape



□ **But we know at least one solution — Hebbian peak.**

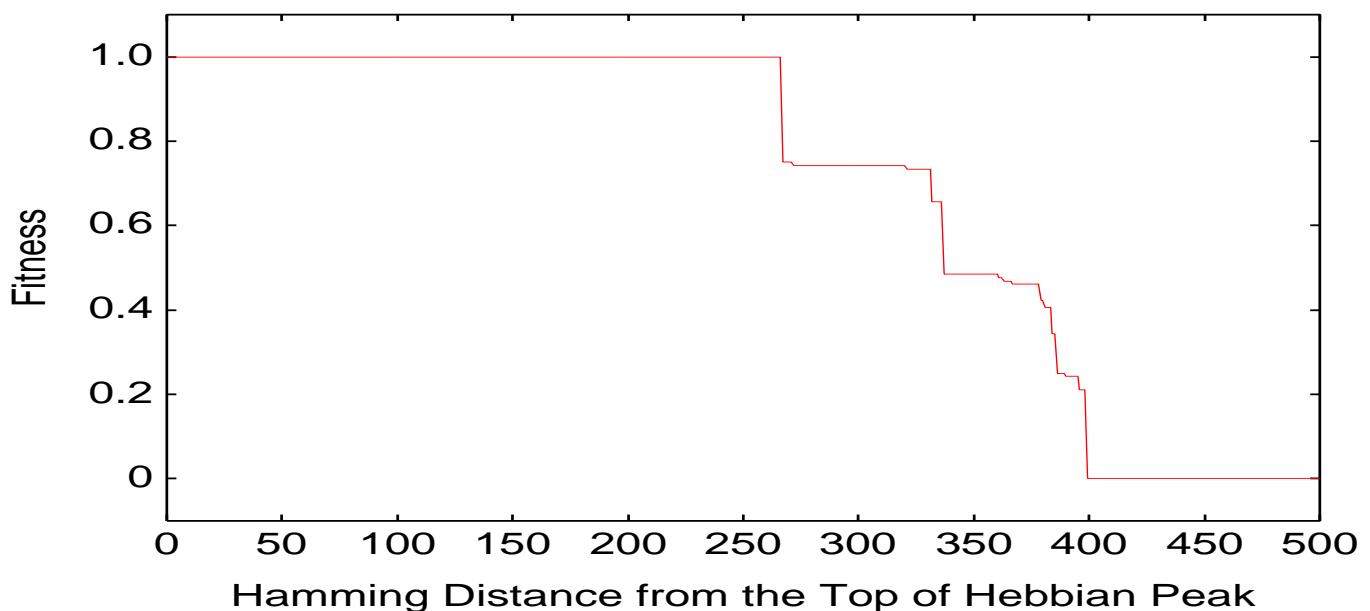
$$w_{ij} = \text{sgn}(R_i - M/2) \cdot \text{sgn}(R_j - M/2)$$

- A Downhill Walk by Flipping zero to one:



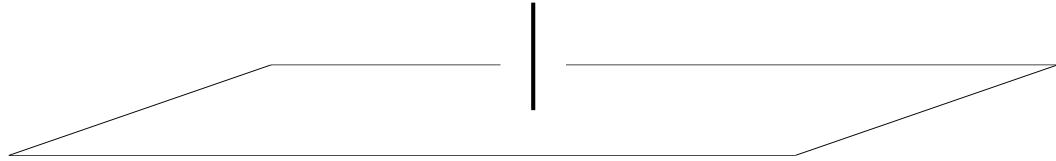
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- **A Downhill Walk by Flipping one to zero:**

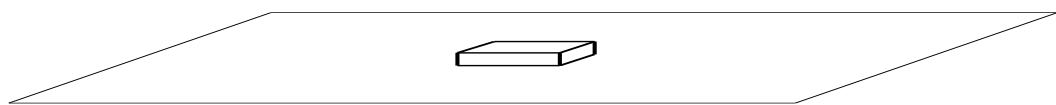


□ Search for a mesa

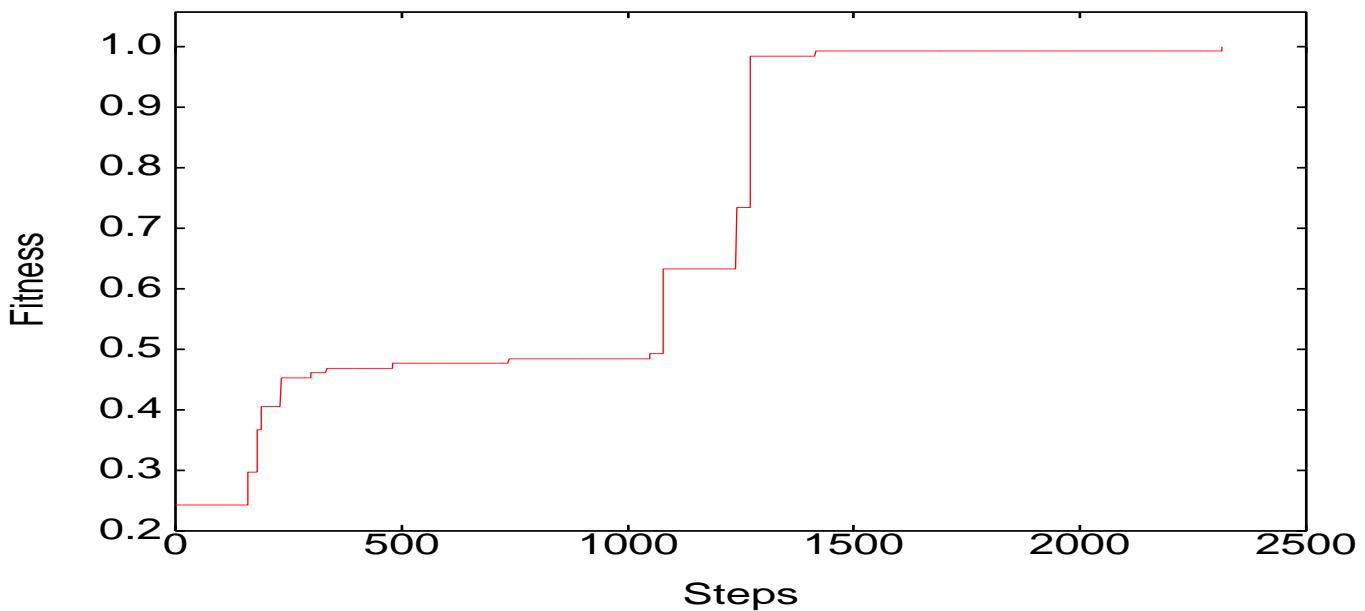
(a) A needle in haystack



(b) A mesa in desert



- Hill climbing from very edge of sidewall.



□ **Hinton & Nowlan's Search for A-needle-in-haystack**

- A-needle \Rightarrow Only one configuration of 20 bits of binary string.
- Haystack $\Rightarrow 2^{20} - 1$ search points.
 - say, (11111111110000000000) is assigned fitness one,
 - while others are fitness zero.

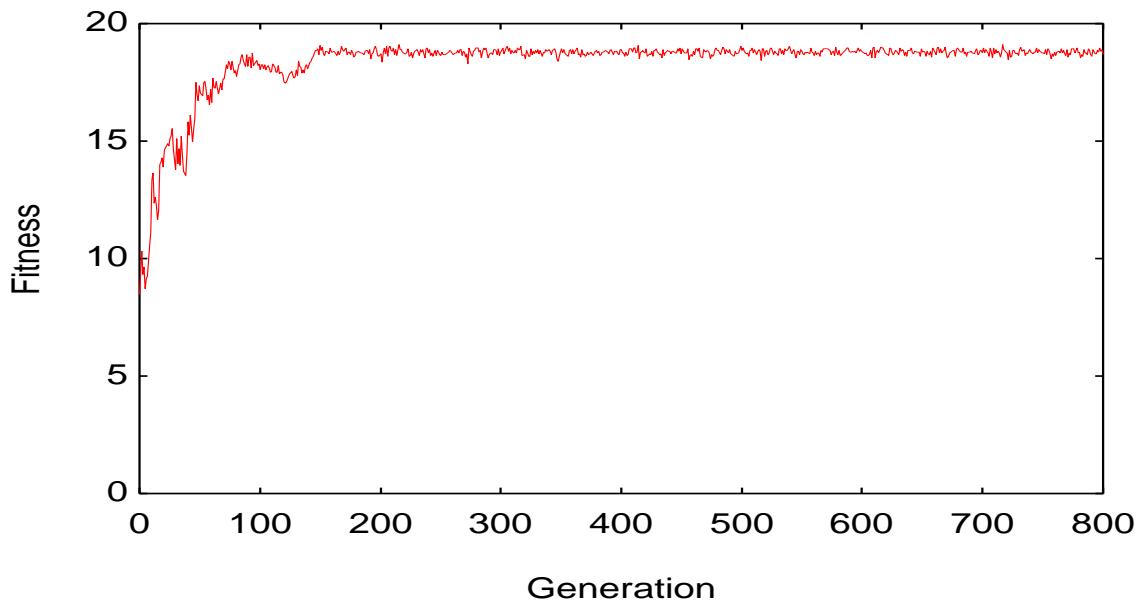
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- **lifetime learning of each individual (Baldwin Effect).**

- about 25% are “1”, 25% are “0”, and the rest of the 50% are “?” .
- They are evaluated with all the “?” position being assigned “1” or “0” at random \Rightarrow *learning*
- Each individual repeats the learning up to 1000 times
- If it reaches the point of fitness one at the n -th trial, then the *degree to which learning succeeded* is calculated as

$$1 + 19 \cdot (1000 - n)/1000.$$

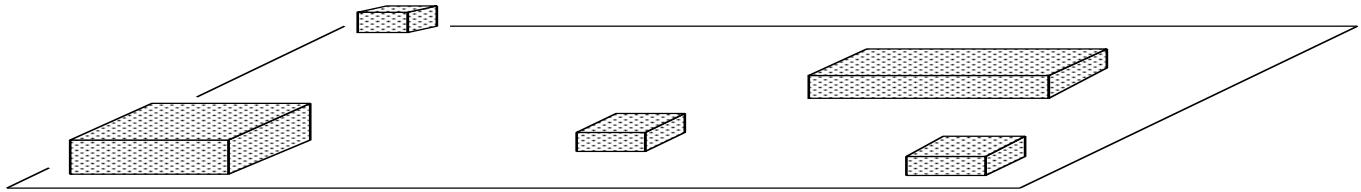
□ Search for a needle



□ Conclusion

- Search for weights to store patterns is as difficult as a search for *a needle in haystack* despite a fairly wide area of top reageon.
- Is it due to very steep side wall of the peak? \Rightarrow *a mesa in a desert!*
- Can climbers take all the way up the steep hillside again? \Rightarrow Yes, but only from the edge.
- Effect of learning during life time (Baldwin Effect) helps us to search for the mesa?

□ Where to go hearafter? — Future Works.



- Peaks other than Hebb's (from NN aspect).
- Search for tiny mesa in desert (from EC aspect).