A-mesa-in-desert vs a-needle-in-haystack:

A fitness landscape on weight space of an application using spiking neurons under rate coding.

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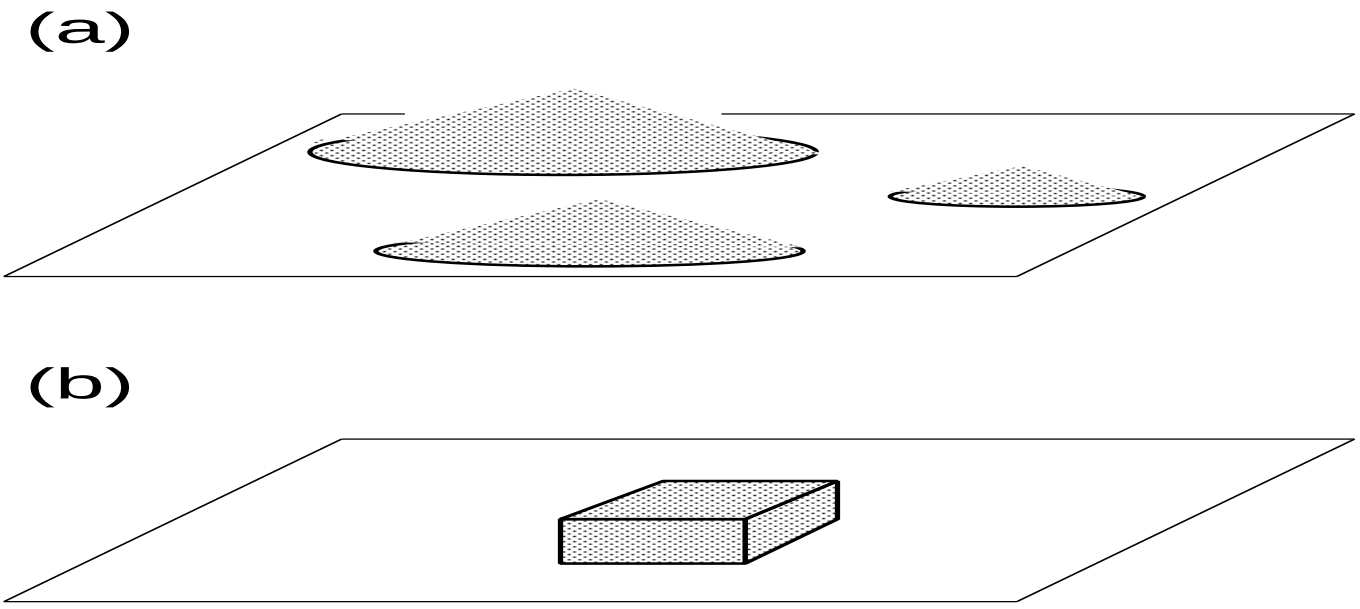
We came accross

an extremely difficult
PEAK
to be searched for

in a
FITNESS LANDSCAPE

explored by an
EVOLUTIONARY COMPUTATION

□ A reason for the title — A mesa in desert



To realize an

ASSOCIATIVE MEMORY

we use

SPIKING NEURONS

whose learning is by

EVOLUTIONARY COMPUTATIONS.

□ Contents

1. What is Associative Memory?

· **Traditional Model by Hopfield.**

vs.

· **A Model using Spiking Neurons.**

2. Can we evolve Spiking Neurons?

· **Study it by Fitness Landscape.**

(cont'd)

3. Results of our Experiments.

- **Let's see a downhill walk from Hebb's peak!**
- **Can we hillclimb again?**
- **Can Baldwin Effect help us to search?**

4. Summary & Conclusions.

□Associative Memory:

- **stores patterns**
  - **– in a distributed way (among neurons),**
- **recalls patterns**
  - **– from noisy and/or partial input.**

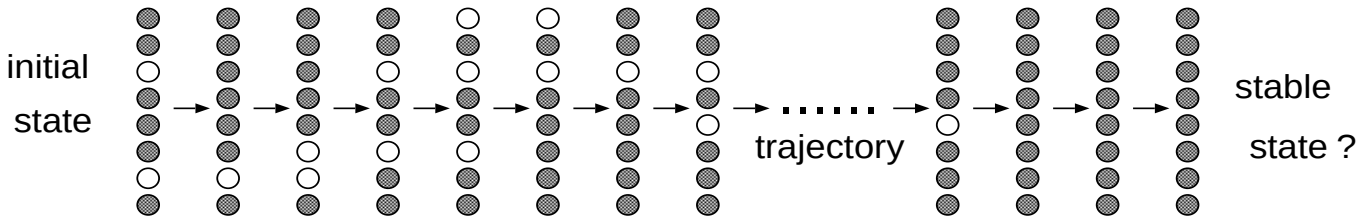
$\Downarrow$ **i.e.**

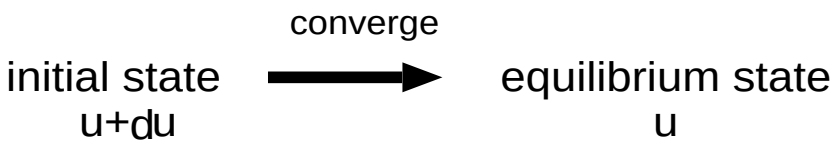
- **gives us**
  - **– perfect recollection from imperfect information**

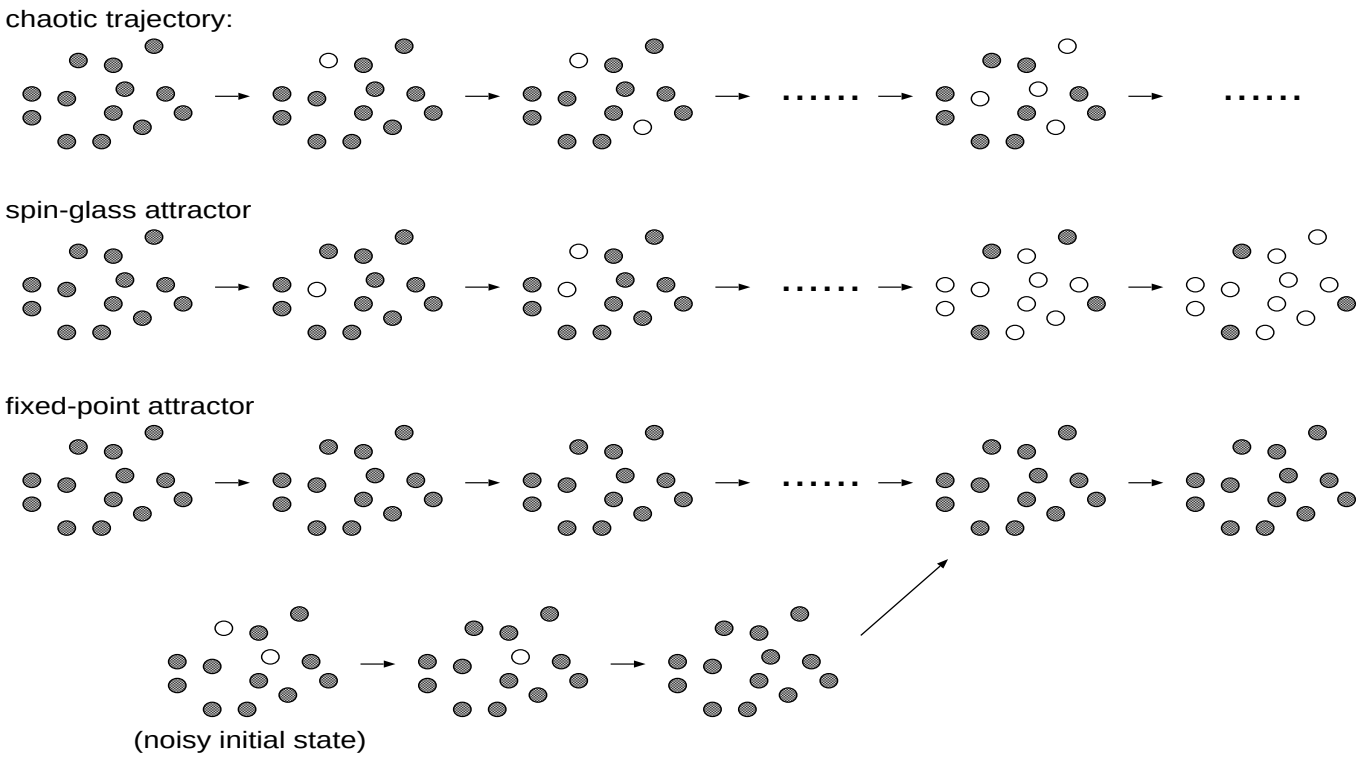
□The Associative Memory can be realized with:

- **Fully-connected Neural Network Model**
  (Hopfield type)
- **Artificial Immune System Model**
- **Spiking Neurons**
  (To be more biologically plausible)
- **etc.**

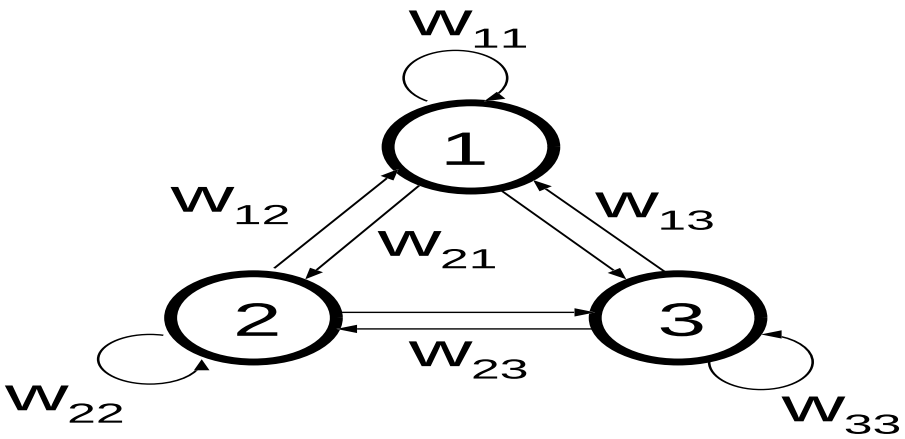
associative memory = dynamical system






chaotic trajectory:
spin-glass attractor
fixed-point attractor
(noisy initial state)

□ A Schematic Diagram of the Hopfield Model



□ State Transition of the Hopfield Model

$$s_i(t+1) = sgn(\sum_{j}^{N} w_{ij} s_j(t))$$

□ Hebbian Weights

$$w_{ij} = \frac{1}{N} \sum_{\mu=1}^{p} \xi_i^\nu \xi_j^\nu, \quad (i \neq j), \quad w_{ij} = 0.$$

(To store p patterns: $\mathbf{x}^\mu = (\xi_1^\mu, \xi_2^\mu, \cdots \xi_N^\mu) \quad \mu = 1, 2, \cdots, p$)

□ Hopfield Model has a Crucial Drawback.

- N neurons store only $2N$ patterns at most (Gardner).

$$p < 2N.$$

□ From the Hopfield Model to Spiking Neuron Model

Influence from other neurons
via
ELECTRIC CURRENTS

⇓

changes
MEMBRANE VOLTAGE
of the neuron.

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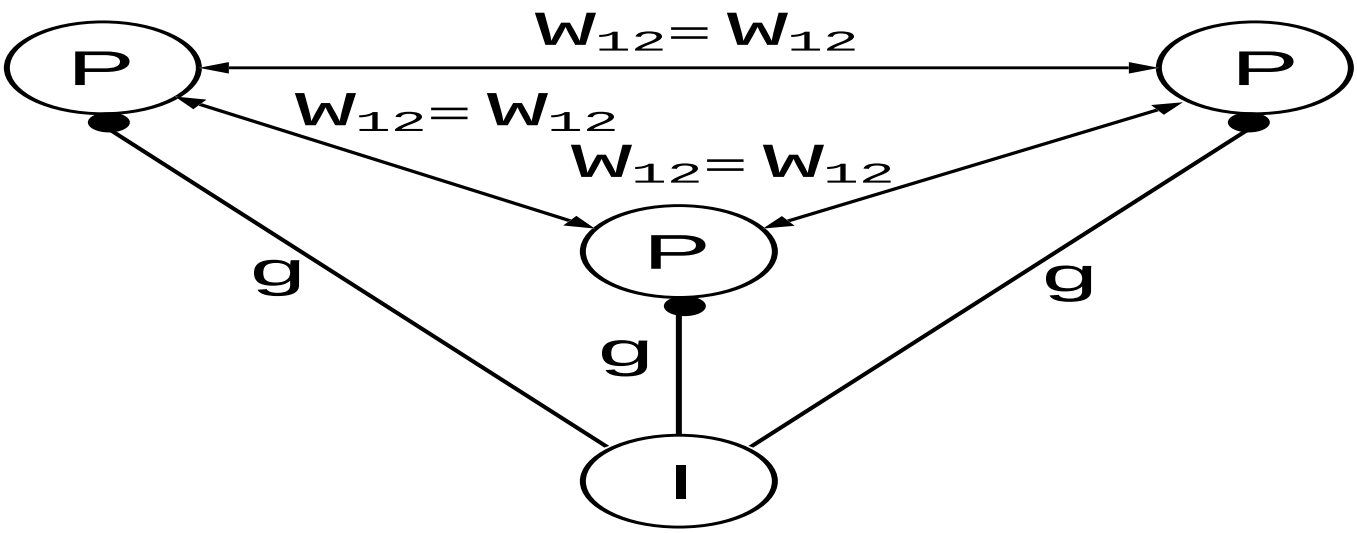
⇓

If it exceeds a threshold

⇓

the neuron emits
a SPIKE.

□ Pyramidal Cells & Interneurons



PYRAMIDAL CELL

$\Vert$

(positive current)

$\Downarrow$

PYRAMIDAL CELL

$\Uparrow$

(negative current)

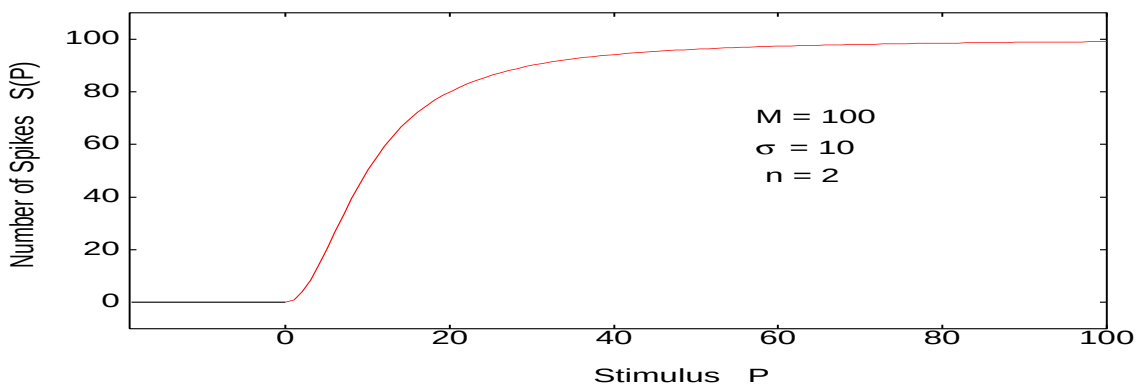
$\Vert$

INTERNEURON

□ Response of a Single Neuron to an External Stimulus:

- **Spike rate vs stimuli (Naka-Rushton function)**

$$S(P) = \begin{cases} MP^n/(\sigma^n + P^n) & \text{if } P \geq 0 \\ 0 & \text{if } P < 0 \end{cases}$$



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- **Spike rate under time-variant stimulus:**

$$\frac{dr(t)}{dt} = \frac{1}{\tau}(-r(t) + S(P))$$

□ Response of Multiple Neurons

• Stimulus to a Pyramidal Cell

$$P_i = (\sum_{j=1}^{N} w_{ij} \cdot R_j - g \cdot G)_+^2$$

of

$$S(P_i) = M P_i^n / (\sigma^n + P_i^n)$$

(cont'd)

- **Spiking Ratio of a Pyramidal Cell**

$$\frac{dr}{dt} = \frac{1}{\tau}(-r + MP^n/(\sigma^n + P^n))$$

becomes

$$\tau_R \frac{dR_i}{dt} = -R_i + \frac{100(\Sigma_{j=1}^{N} w_{ij} R_j - 0.1G)_+^2}{100 + (\Sigma_{j=1}^{N} w_{ij} R_j - 0.1G)_+^2}$$

(cont'd)

- **Spiking Ratio of Interneuron**

$$\tau_G \frac{dG}{dt} = -G - 0.07 \sum_{j=1}^{N} R_i$$

□ How to encode patterns?

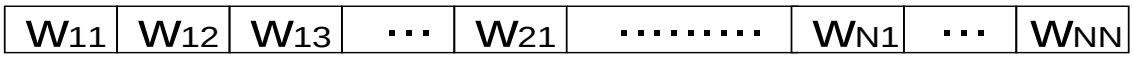
$$\xi_i = \begin{cases} 1 & \text{if } R_i \geq M/2 \\ 0 & \text{if } R_i < M/2 \end{cases}$$

$\Rightarrow$ Rate Coding

- Rate Coding
- Time Coding

□ GA Implementation:

1. Represent a series of w_{ij} as a *population* of strings (*chromosome*).



2. Evaluate *fitness* by "How good is each individual?"
3. Generate an initial *population* at random.

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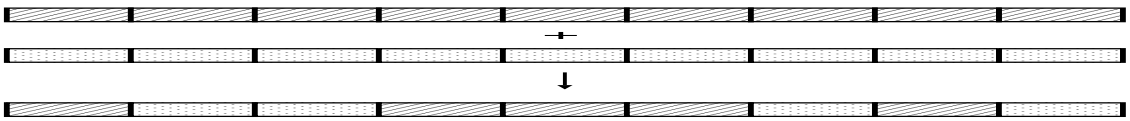
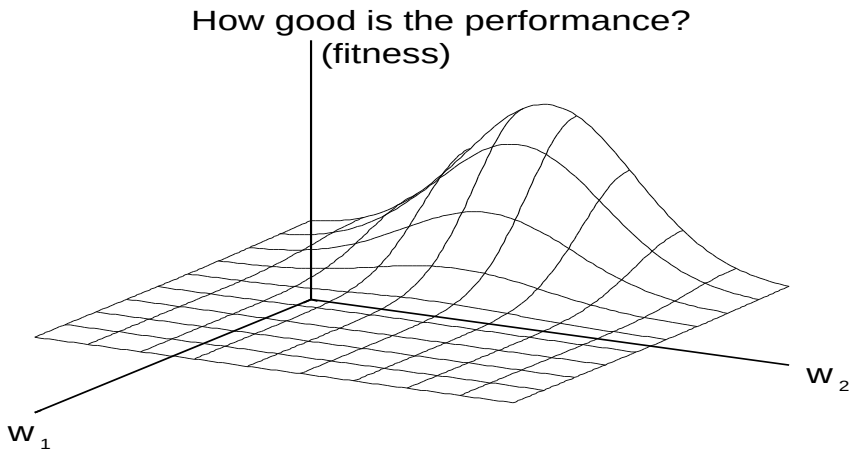
4. Evolve them with
   - *Selection*
   - *Crossover*



   - *Mutation*

5. Better Solutions from *generation* to *generation.*

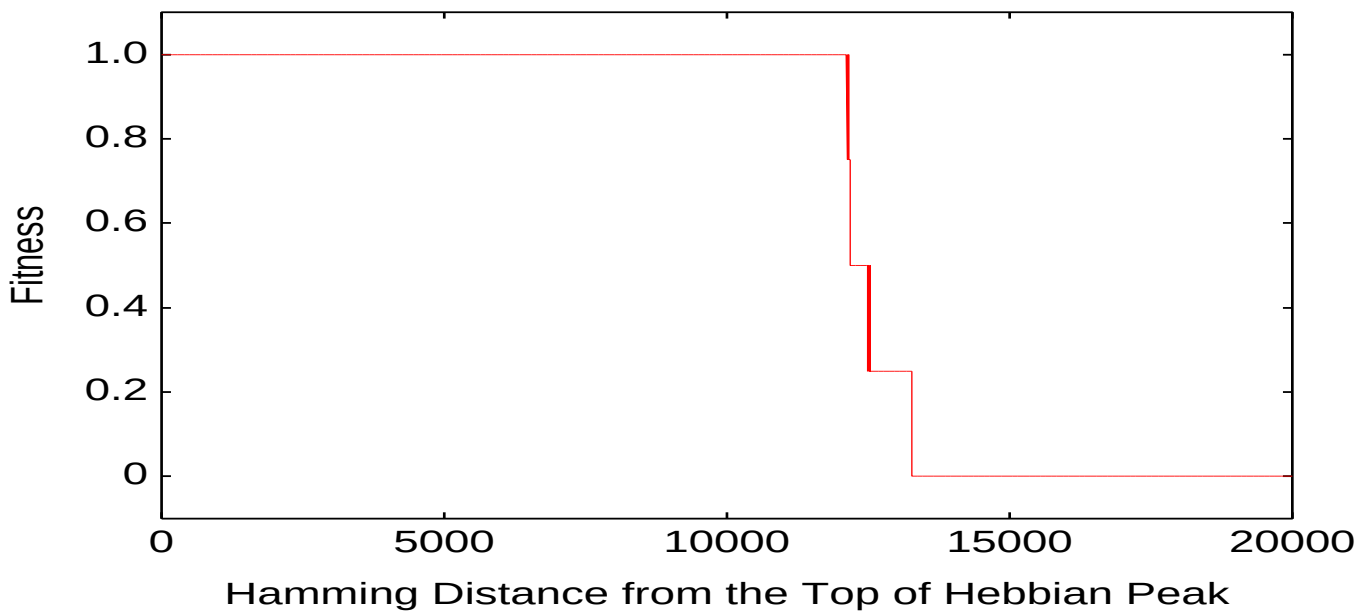
□ A Conceptual Illustration of Fitness Landscape



□ Weights by Hebb's Rule

$$w_{ij} = sgn(R_i - M/2) \cdot sgn(R_j - M/2)$$

- **A Downhill Walk by Flipping zero to one:**



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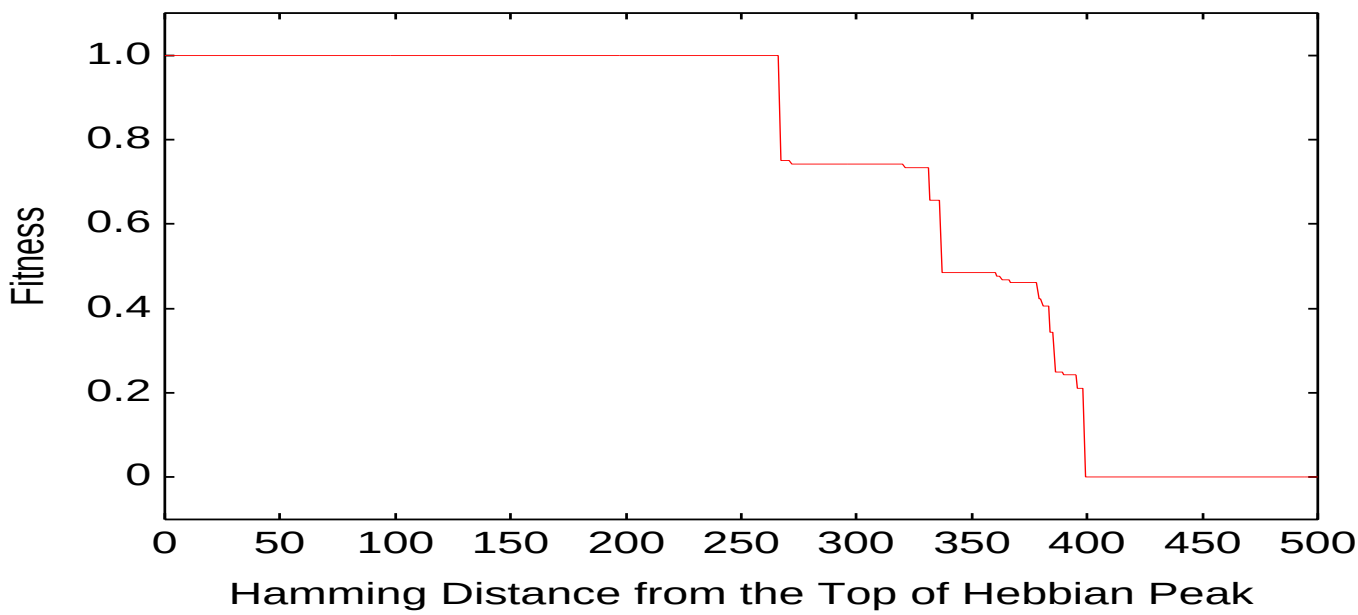
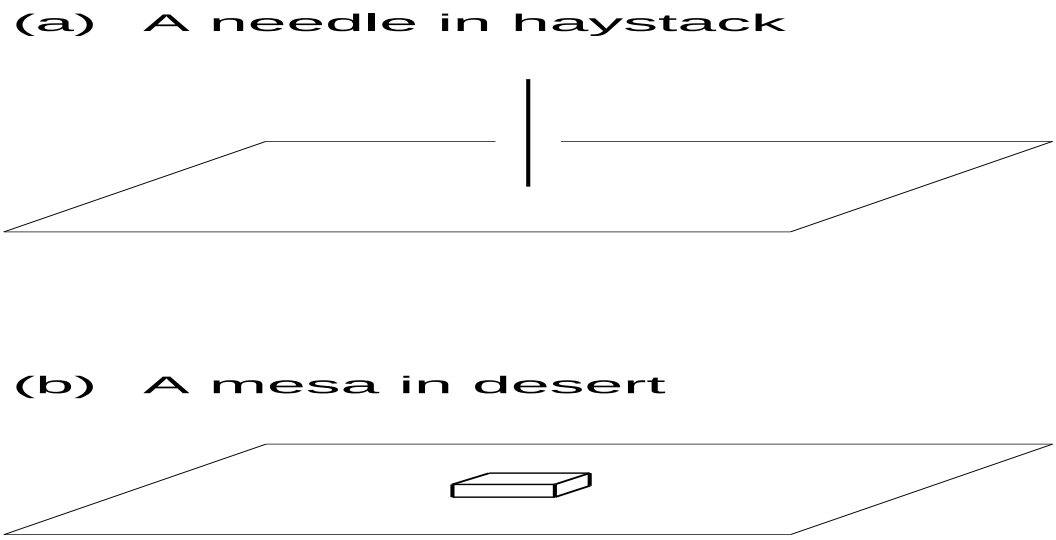
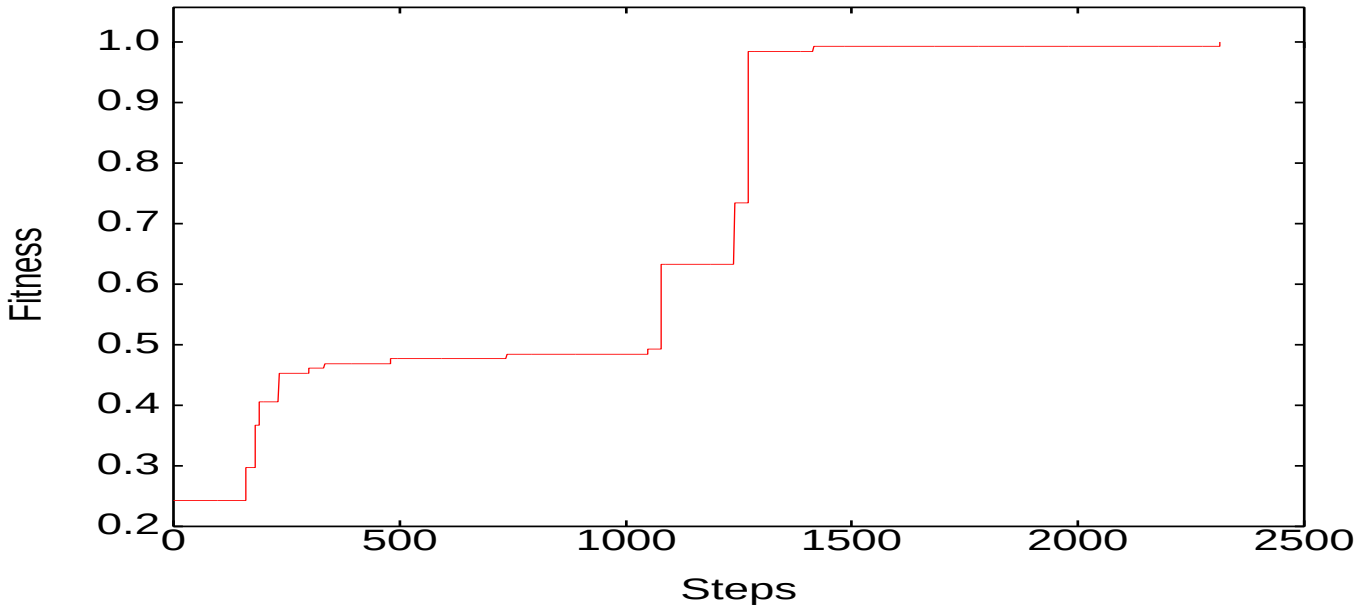
- **A Downhill Walk by Flipping one to zero:**



□ Search for a mesa



□ **Hill climbing from very edge of sidewall.**



□ Hinton & Nowlan's Search for A-needle-in-haystack

- A-needle ⇒ Only one configuration of 20 bits of binary string.
- Haystack ⇒ 2^{20} search points.
  - say, (11111111110000000000) is assigned fitness one, while others zero.

(cont'd)

- **lifetime learning of each individual (Baldwin Effect).**

  · about 25% are "1", 25% are "0", and the rest of the 50% are "?" .

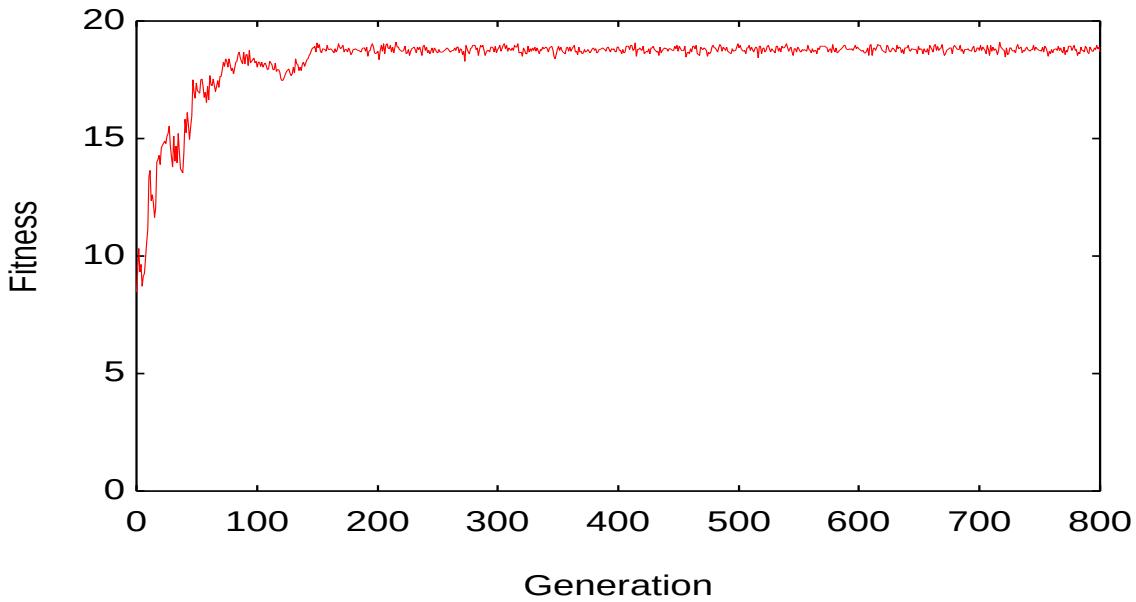
  · They are evaluated with all the "?" position being assigned "1" or "0" at random $\Rightarrow$ *learning*

  · Each individual repeats the learning up to 1000 times

  · If it reaches the point of fitness one at the n-th trial, then the *degree to which learning succeeded* is calculated as

$$1 + 19 \cdot (1000 - n)/1000.$$

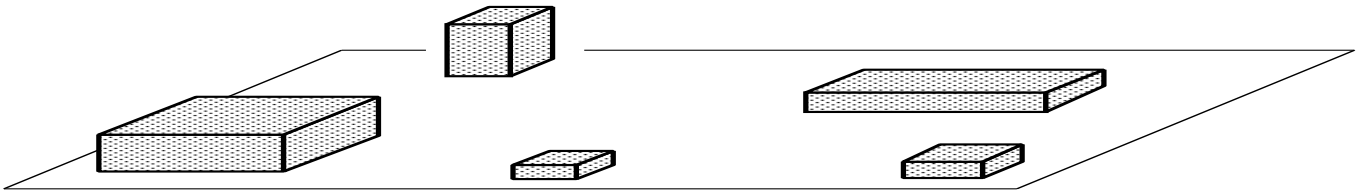
□ Search for a needle



□ Conclusion

- Search for weights to store patterns is more difficult than a search for
  - · a needle in haystack.
- We guess it's due to very steep side wall of the peak.
  - · A mesa rather than a peak?
- Can climbers take all the way up the steep hillside again?
  - · Yes, but only from the edge.
- Hinton & Nowran's Experiment?
  - · Effect of learning during life time (Baldwin Effect).

□ Where to go hearafter? — Future Works.



- Peaks other than Hebb's (from NN aspect).
- Search for tiny mesa in desert (from EC aspect).